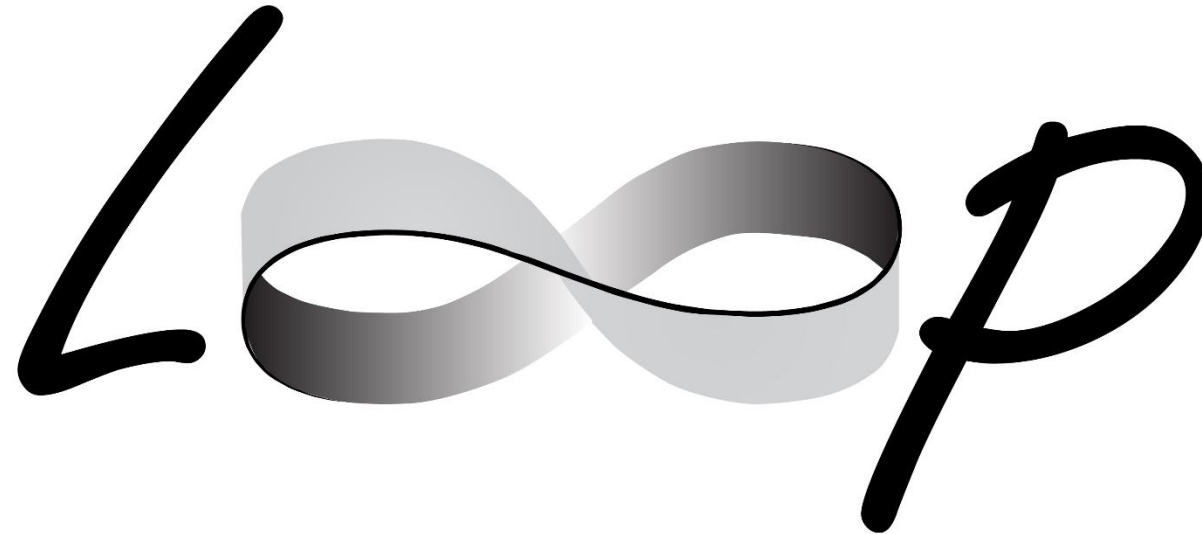


## School of Earth, Atmosphere and Environment



L. AILLERES, M. JESSELL, E. DE KEMP, G. CAUMON, F. WELLMANN, S. LOPEZ, M. HILLIER, G. LAURENT, G. COURRIOUX<sup>6</sup>, E. SCHETSELAAR, R. ARMIT, M. LINDSAY, P. CALCAGNO, P. COLLON, B. BRODARIC, C. LOISELET, T. CUI, J. DRONIOU, P. G BETTS, F. BONNEAU, A.R. CRUDEN, and many others...



Government of **Western Australia**  
Department of Mines and Petroleum



Australian Government  
Geoscience Australia



MONASH University



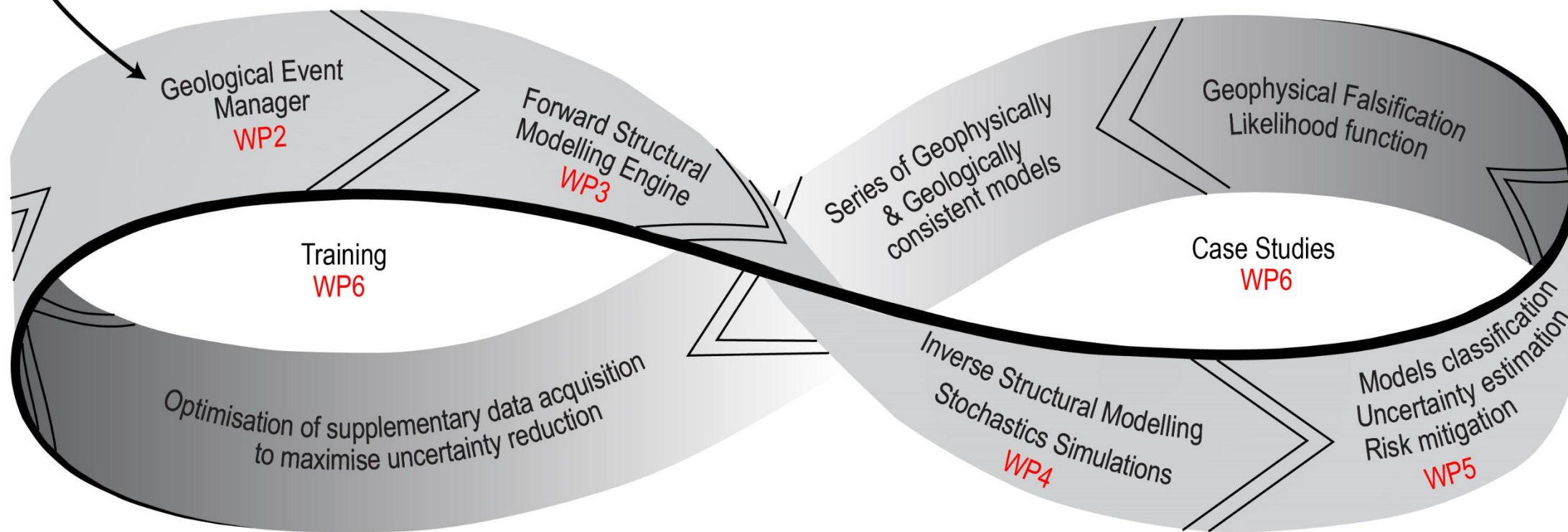
THE UNIVERSITY OF  
WESTERN  
AUSTRALIA



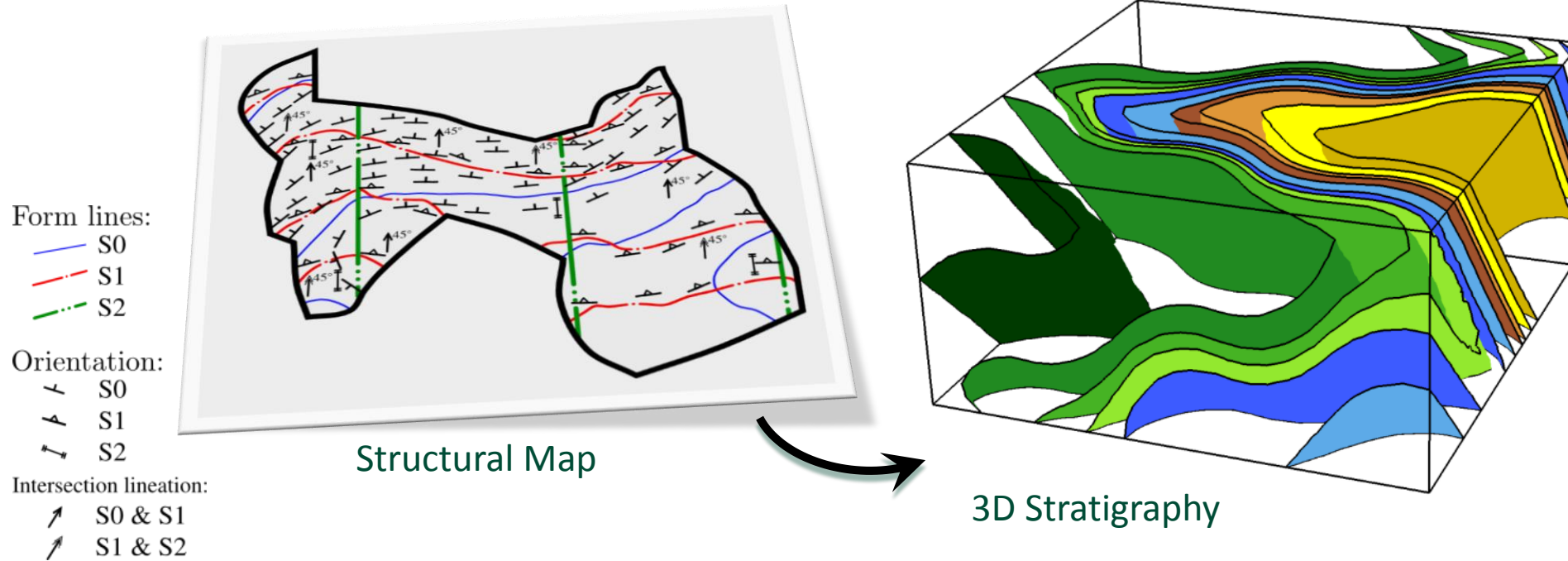
RWTHAACHEN  
UNIVERSITY



Input Geological data and geophysical interpretations & models



- Structural data
- Geological knowledge



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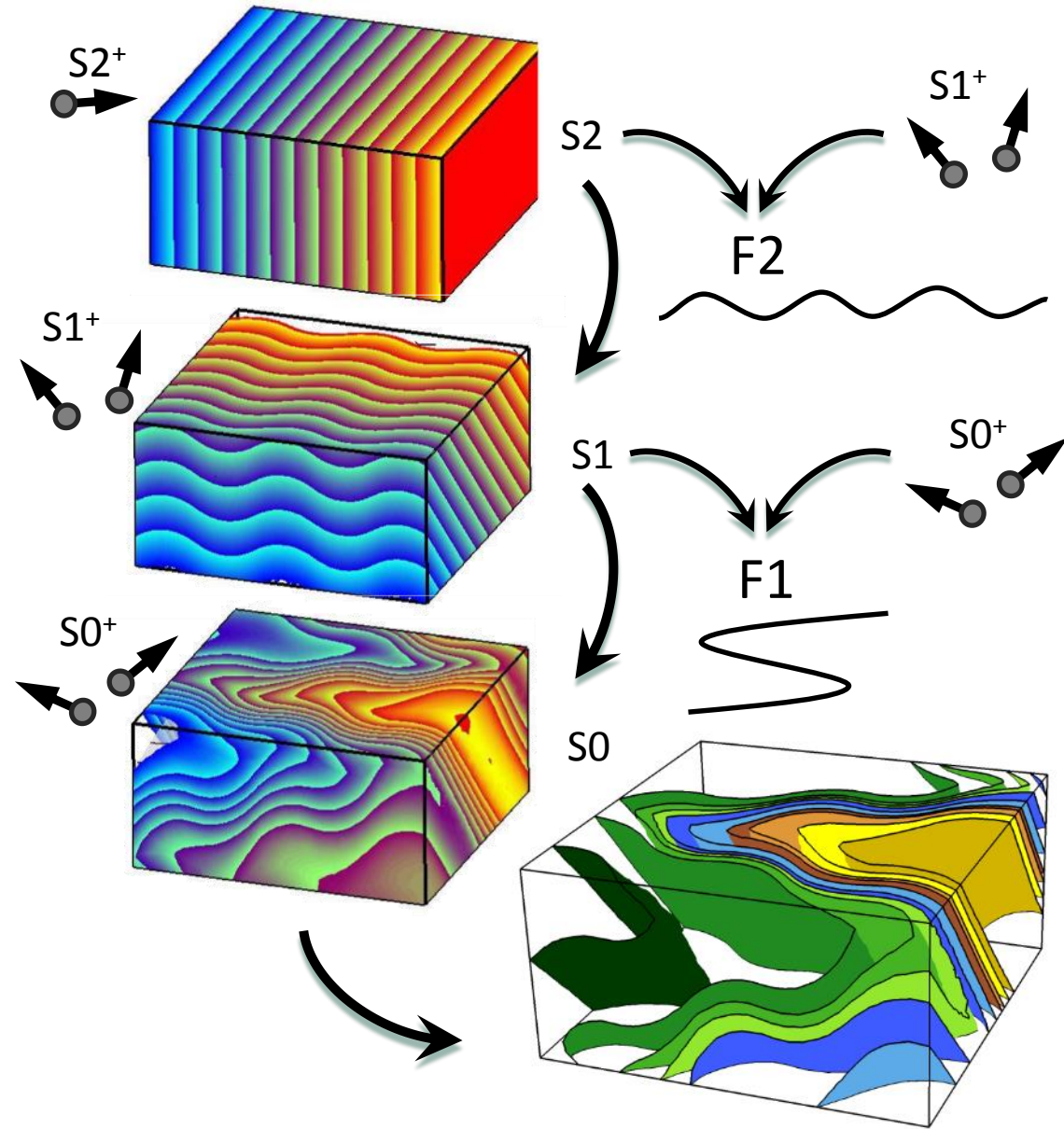


Implicit modeling of folds and overprinting deformation

Gautier Laurent<sup>a,b,\*</sup>, Laurent Ailleres<sup>a</sup>, Lachlan Grose<sup>a</sup>, Guillaume Caumon<sup>b</sup>, Mark Jessell<sup>c</sup>, Robin Armit<sup>a</sup>



1. Poly-deformation:
  - Model step by step
  - Restoration approach
    - going backward in time
  - Fold operator:
    - $S_{i-1} = F_i(S_{i-1}^+ | P_i)$
2. Fold characterisation:
  - Statistics from data
  - Fold Frames
    - Using structural elements
  - Fold Profiles

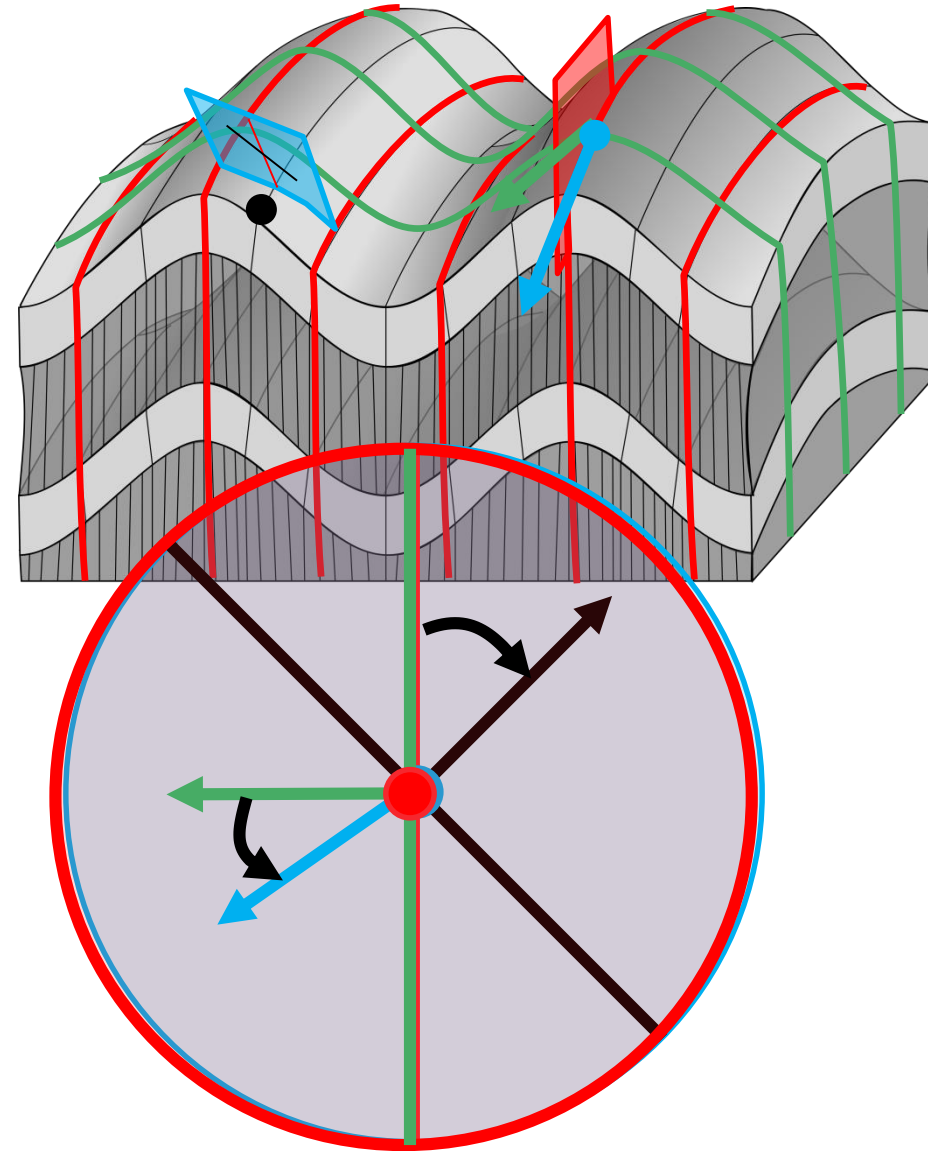


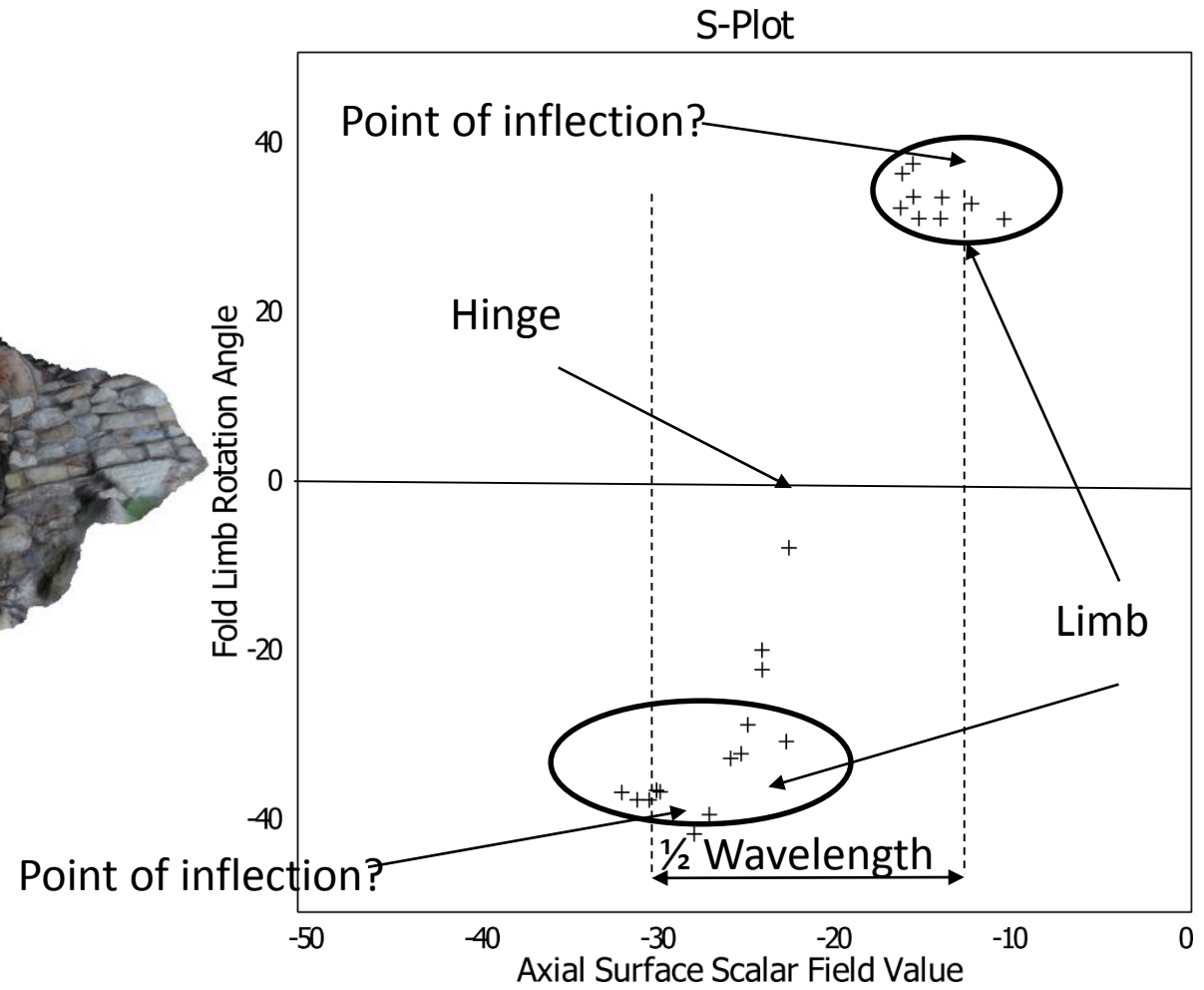
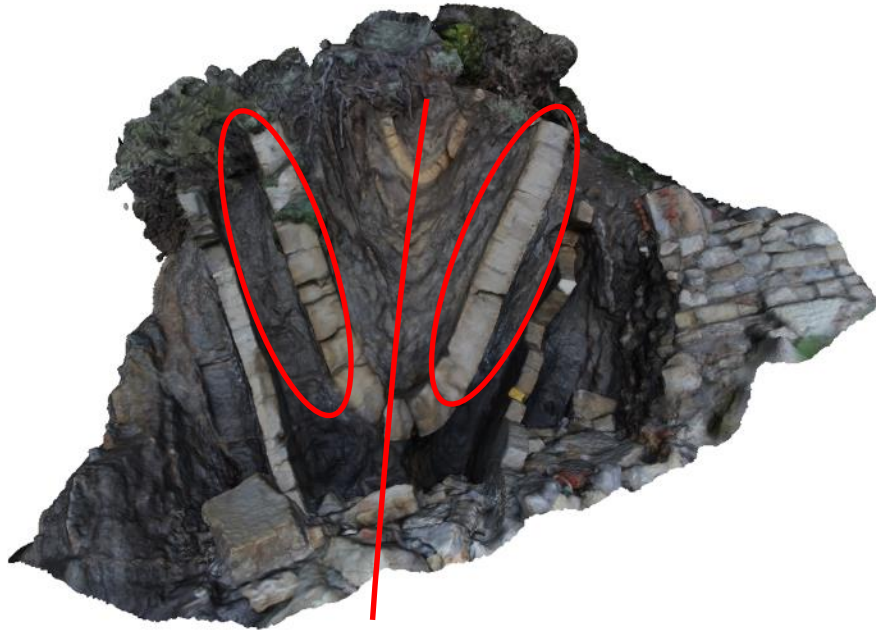
**!! No deformation simulation**  
**!! Only geometric relationship**



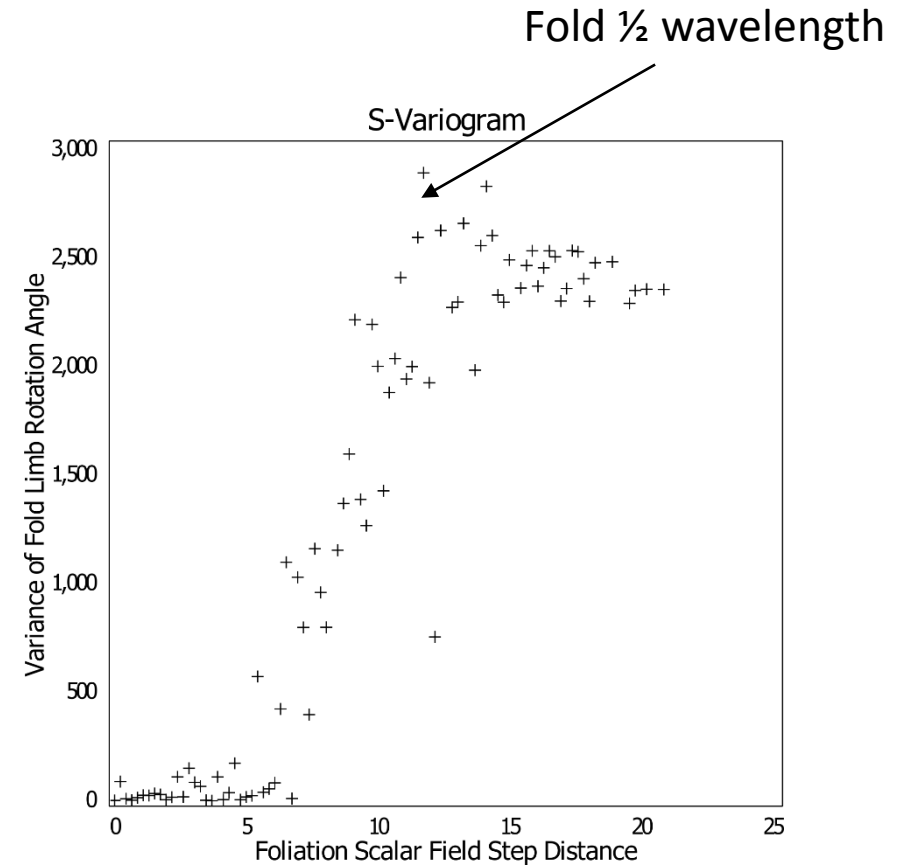
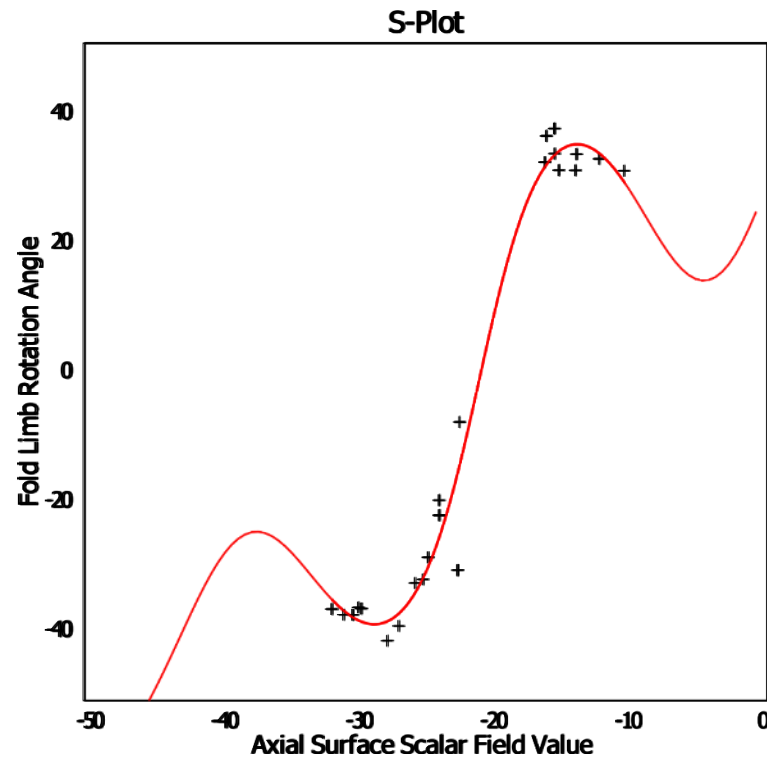


- Fold Axis Rotation Angle
  - Fold axis observation
  - Gradient of Y field
  - In (axial foliation) XY plane
- Fold Limb Rotation Angle
  - Folded foliation observation
  - Gradient of axial foliation (Z field)
  - Looking down plunge

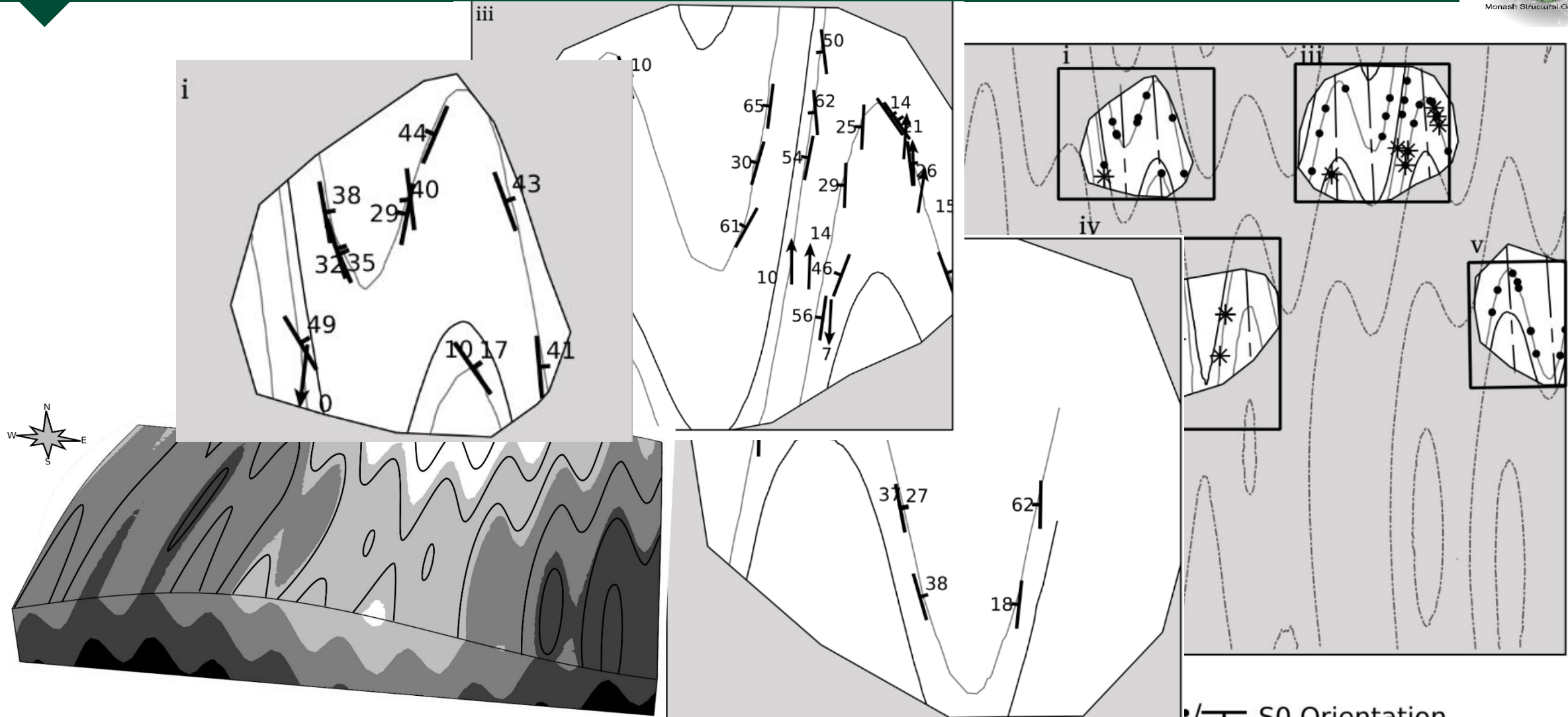




- Interpolate gradient directly instead of angle
- Use fold wavelength as shape parameter



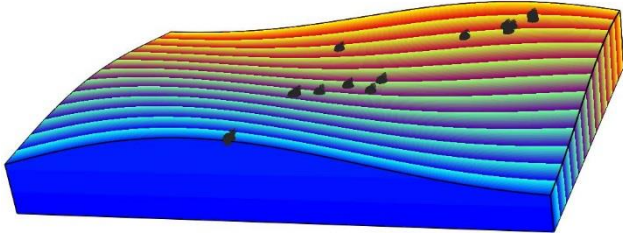
# Today's case study



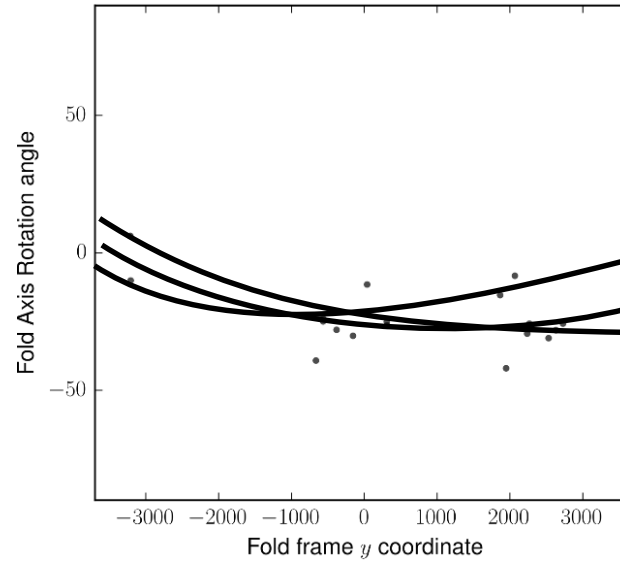
• / — S0 Orientation  
 — S0 Form Lines      - - - - S0 reference model  
 \* / — F1 Orientation      — S1 Form Lines



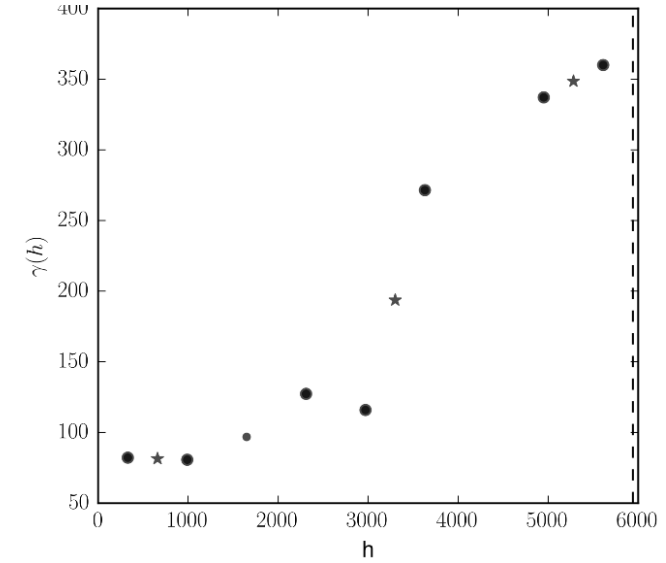
Fold frame y coordinate



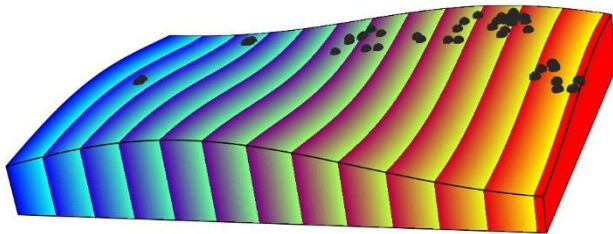
Fold Axis S-Plot



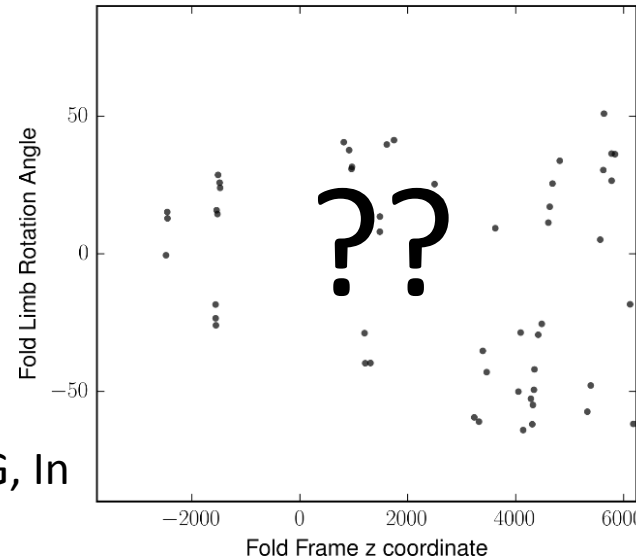
Fold Axis S-Variogram



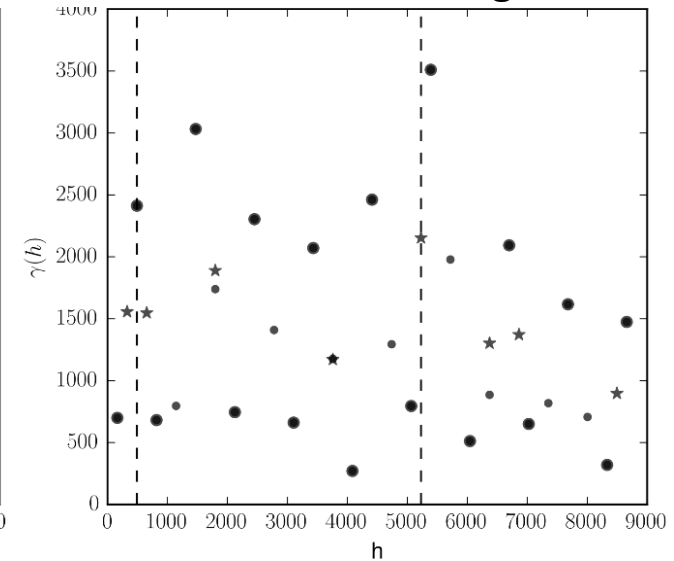
Fold frame z coordinate



Fold Limb S-Plot



Fold Limb S-Variogram



(Grose et al., 2017, JSG, In Press)

- Parasitic folds modelled specifying multiple wavelength parameters

$$\hat{y}(x_i | A_0, A_{1..n}, \lambda_{1..n}) = A_0 + \sum_{n=1}^N B_n \cos \frac{2\pi}{\lambda_n} x_i + \sum_{n=1}^N A_n \sin \frac{2\pi}{\lambda_n} x_i + \text{uncertainty}$$

- Bayesian inference

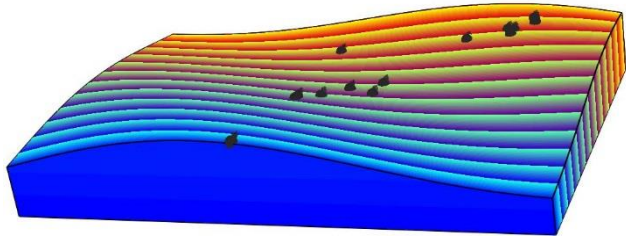
$$P(\theta | D) \propto P(D | \theta) \cdot P(\theta)$$

- Prior distributions:

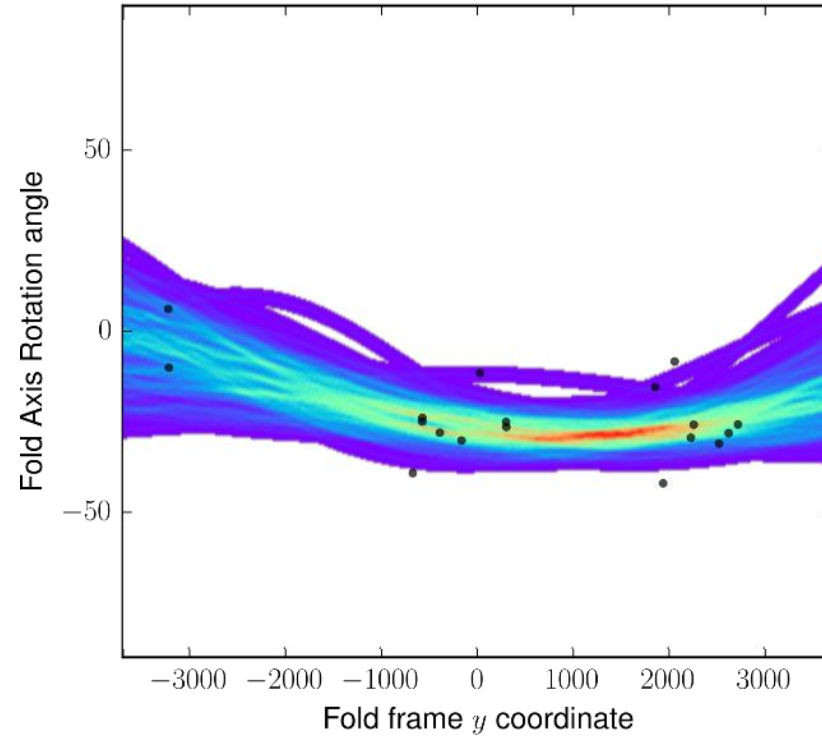
- Fourier coefficients – Normal distribution
- Wavelength – Normal distribution
- Uncertainty – Jeffery's prior (uninformative)

- Sample from joint posterior distribution using Gaussian likelihood function and Markov Chain Monte-Carlo sampler using PyMC2
- Find joint posterior distribution for BOTH rotation angles

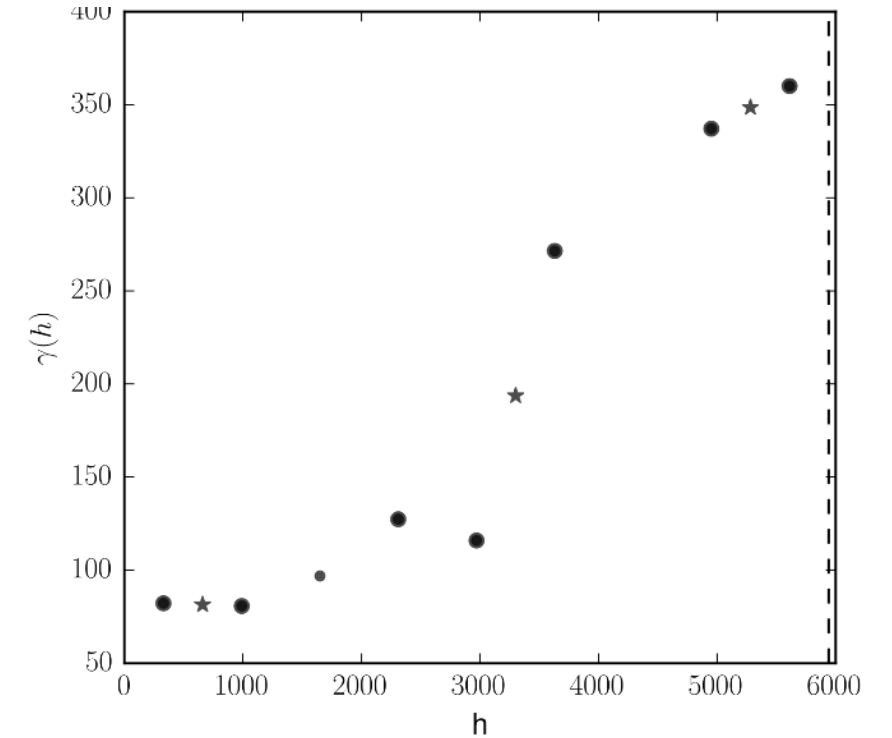
# Fold axis rotation angle



### Fold Axis S-Plot

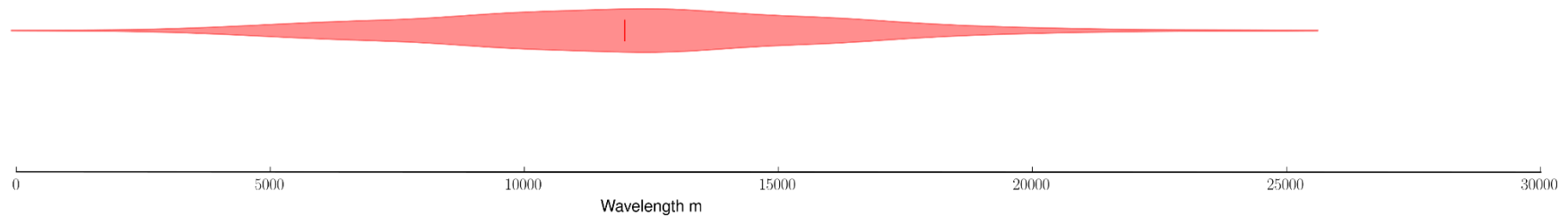


### Fold Axis S-Variogram

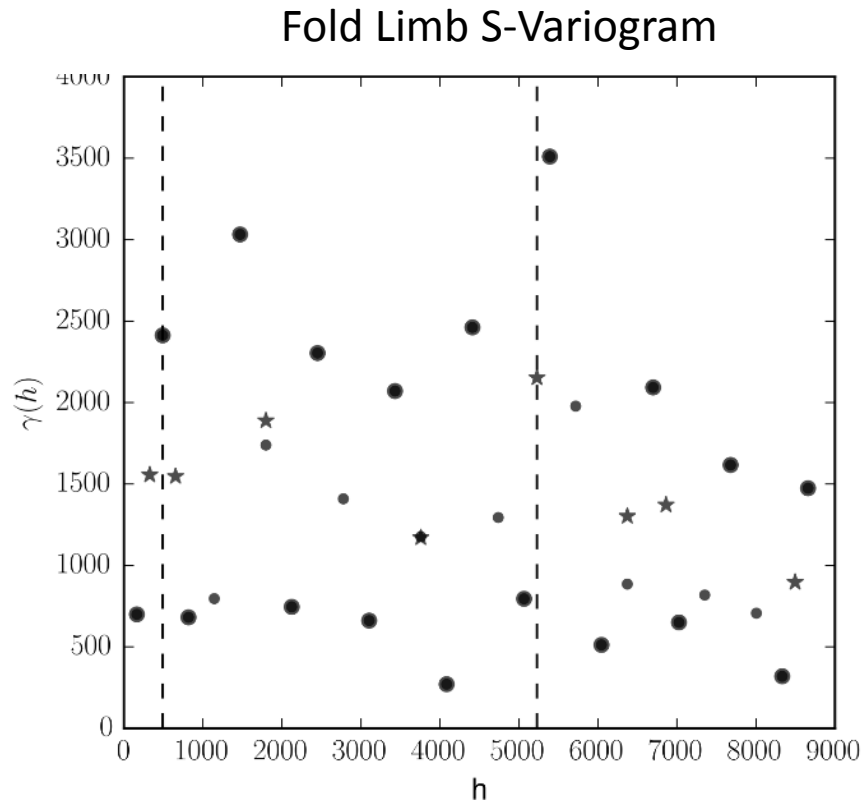
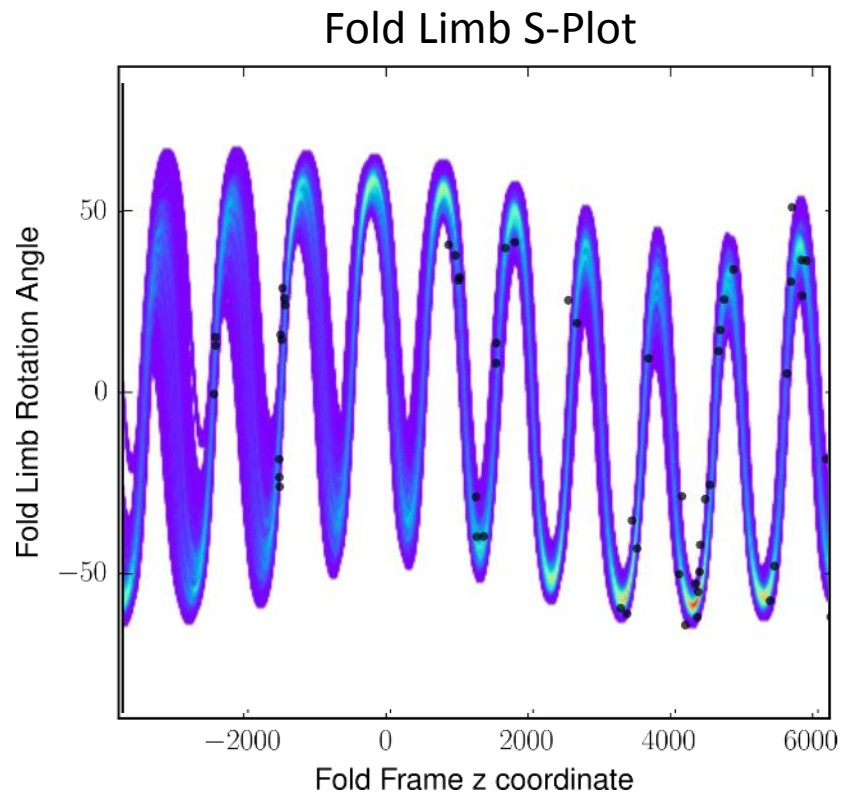
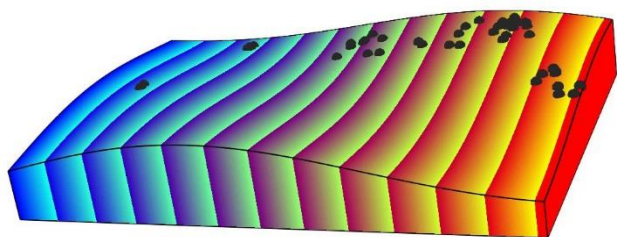


### Wavelength PDF

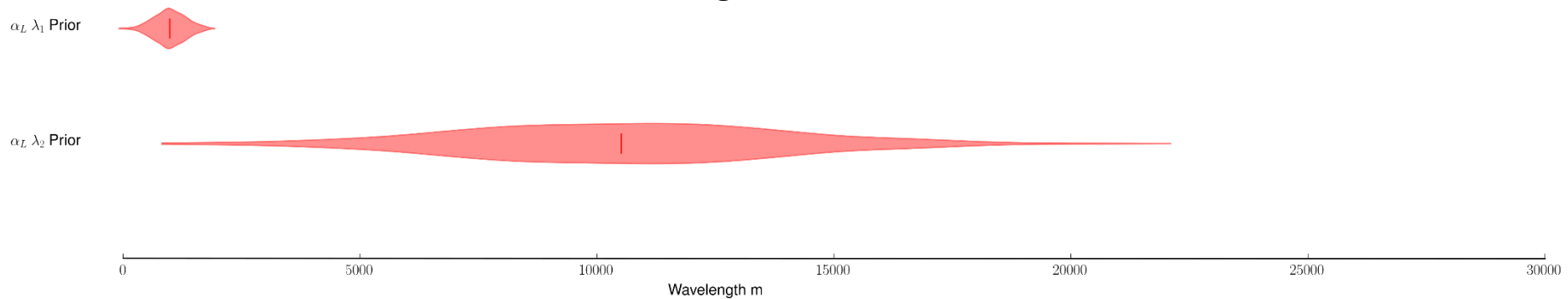
$\alpha_P \lambda$  Prior

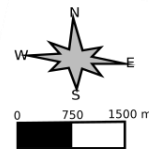
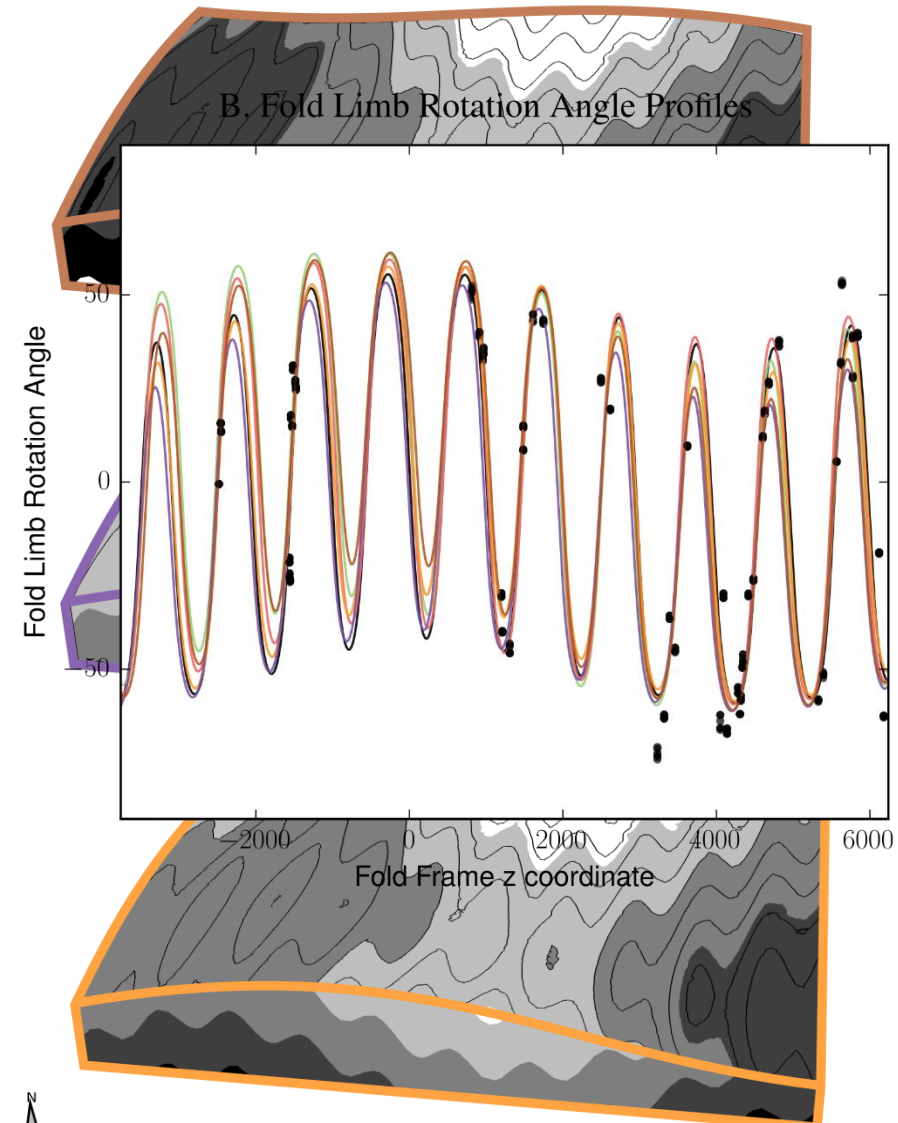
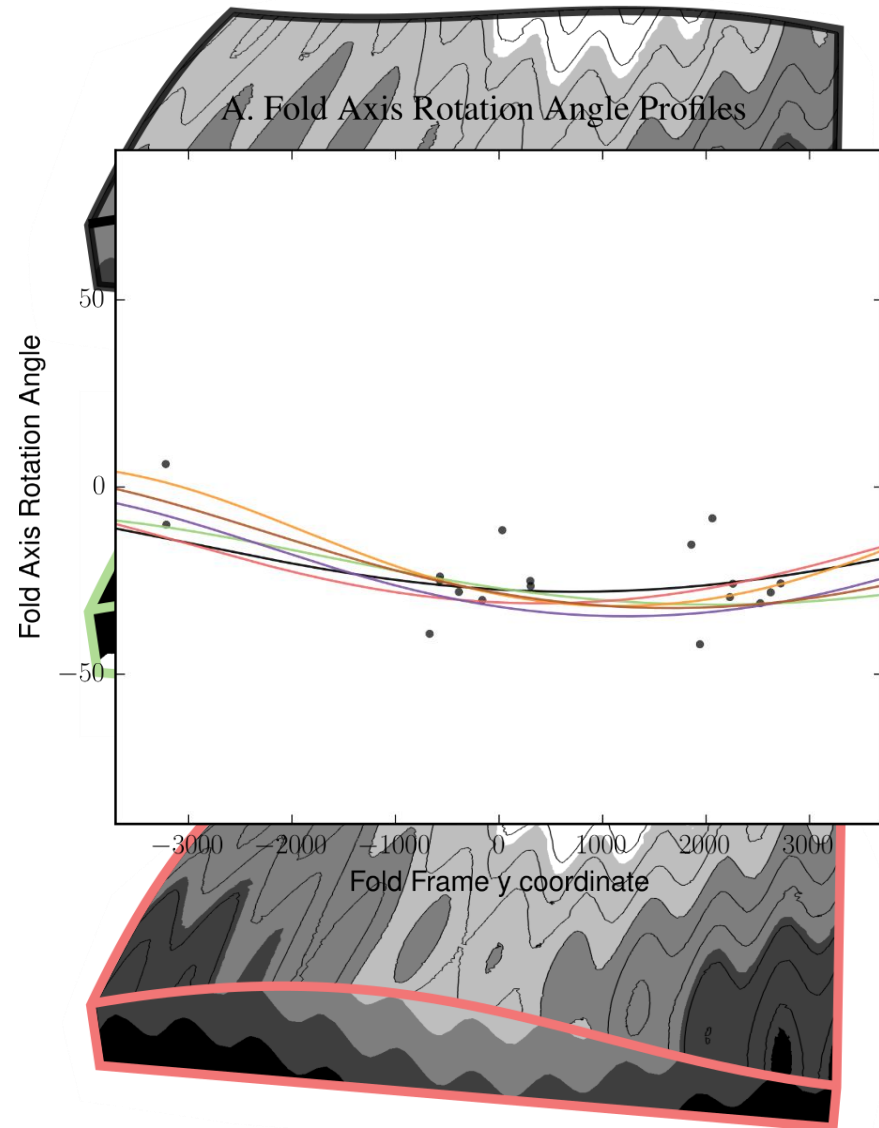


# Fold Limb Rotation angle



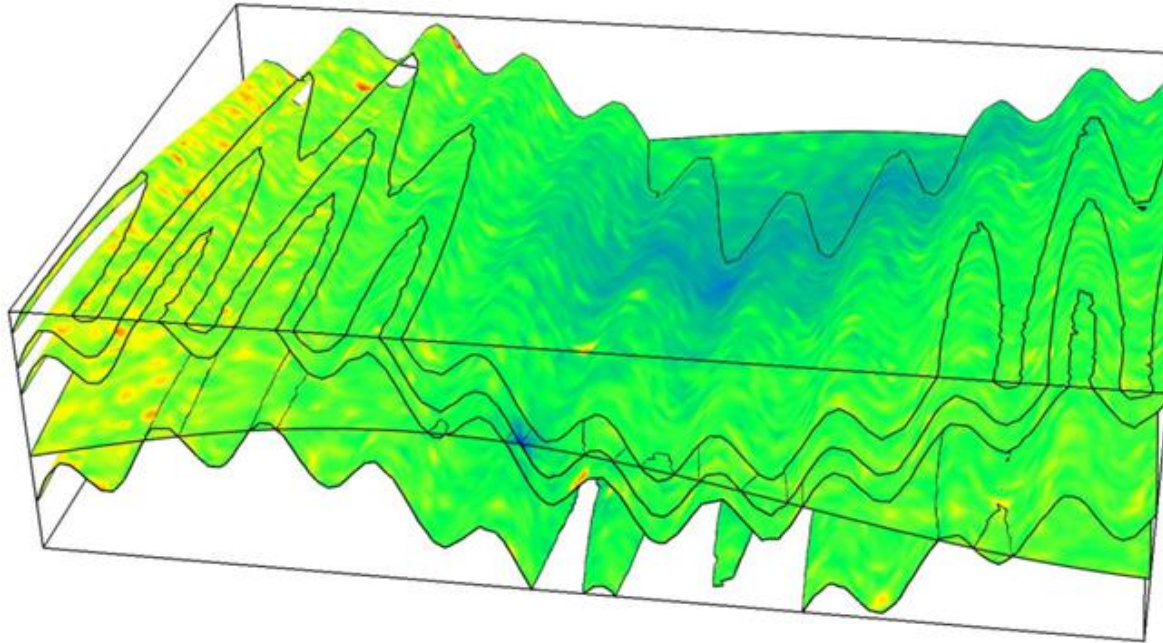
## Wavelength PDFs



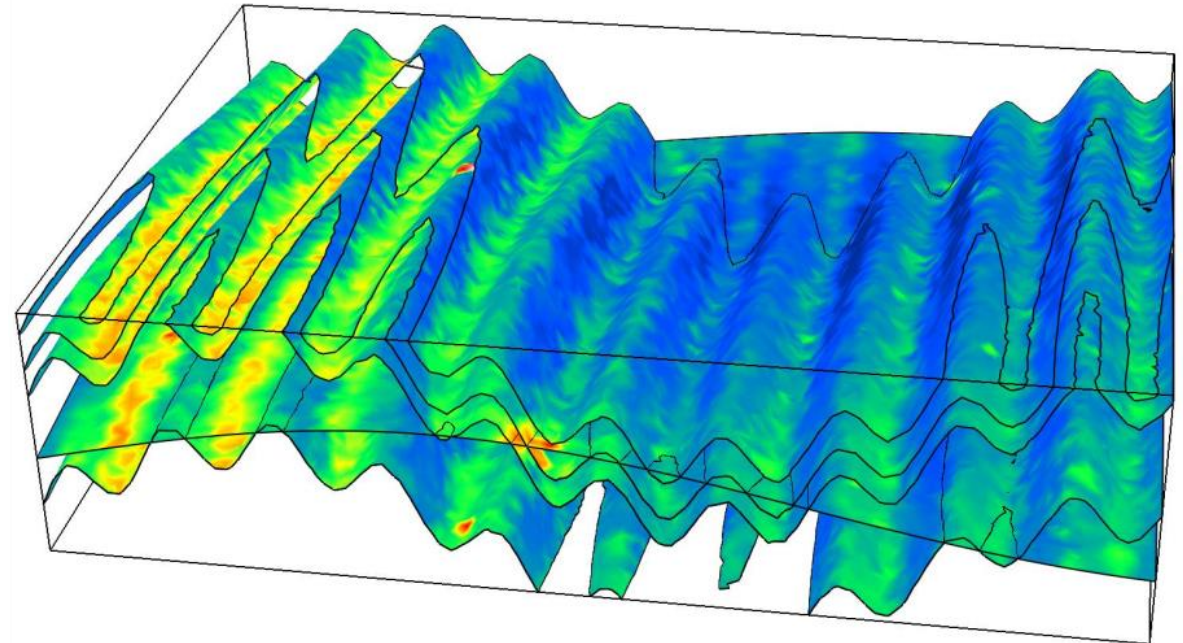


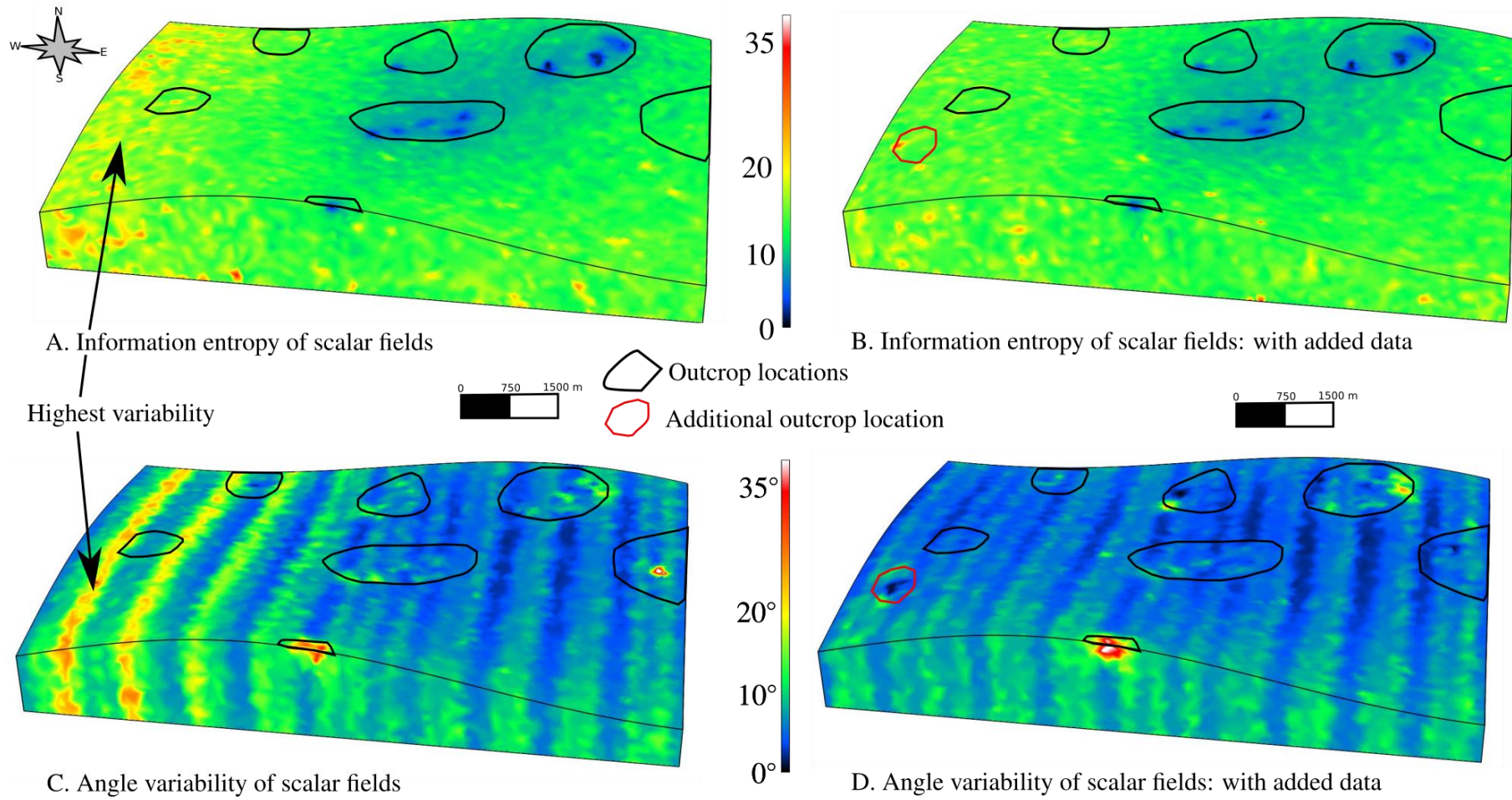


Uncertainty in scalar field value



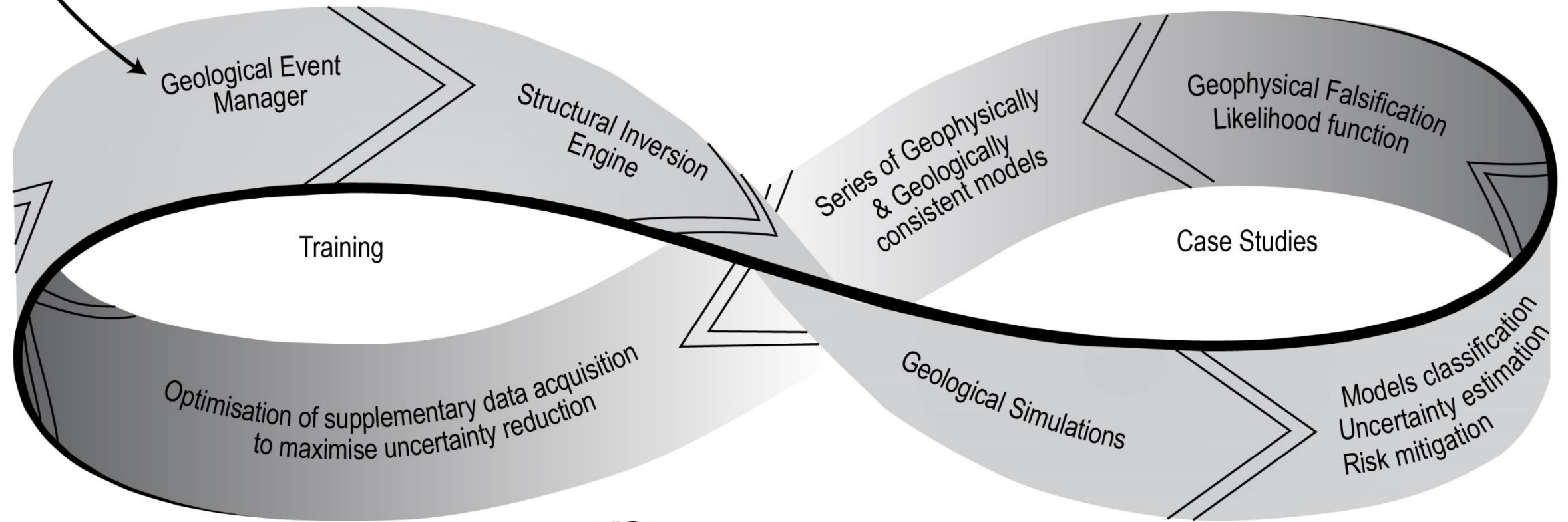
Uncertainty in scalar field geometry





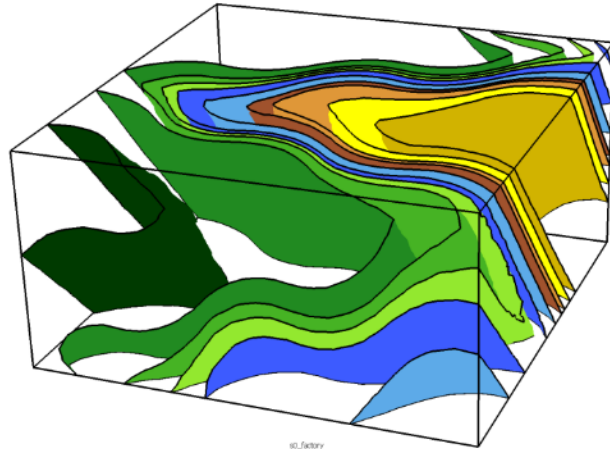


Input Geological data and geophysical interpretations & models

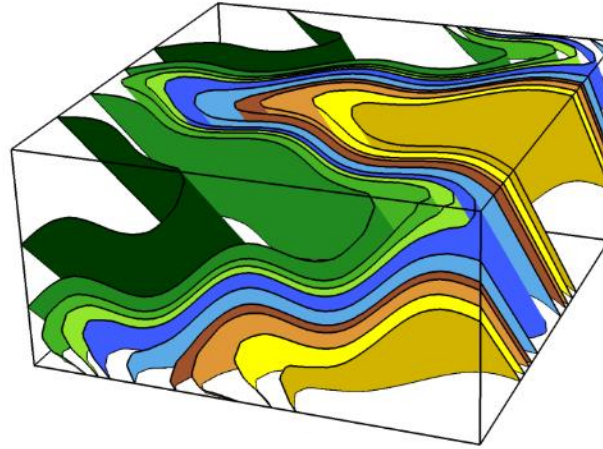


- Measuring differences

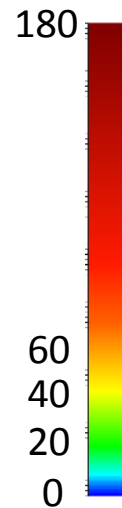
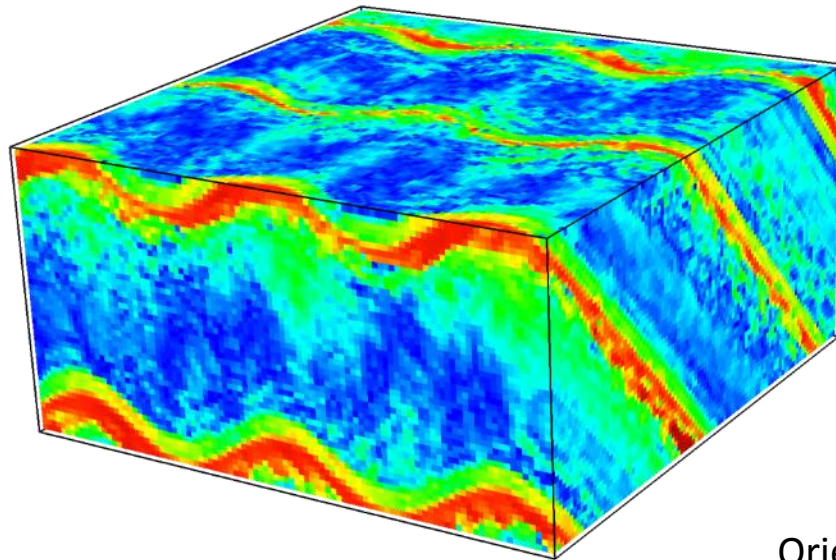
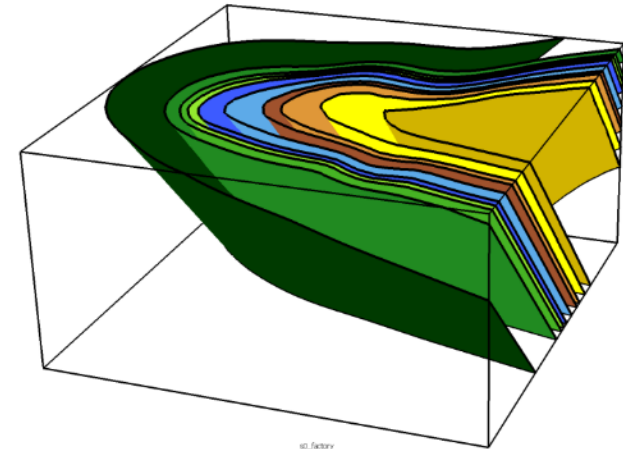
Fold Modelling



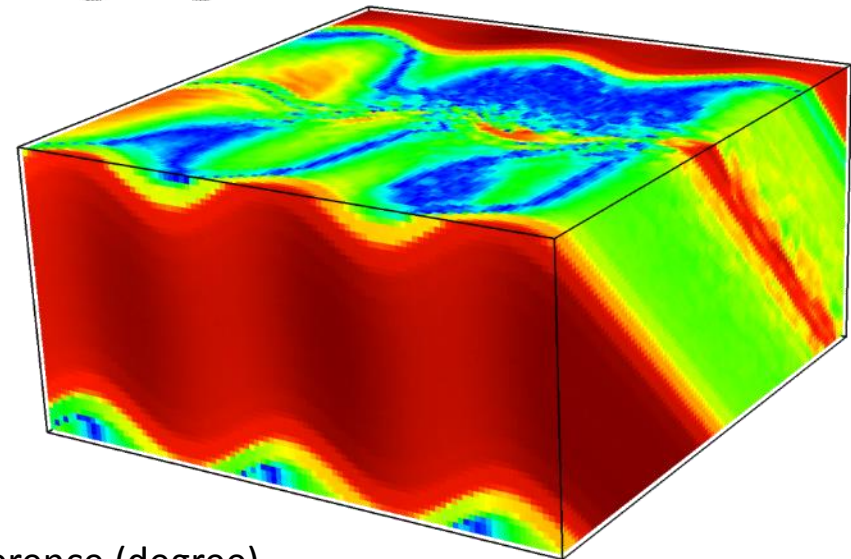
Reference



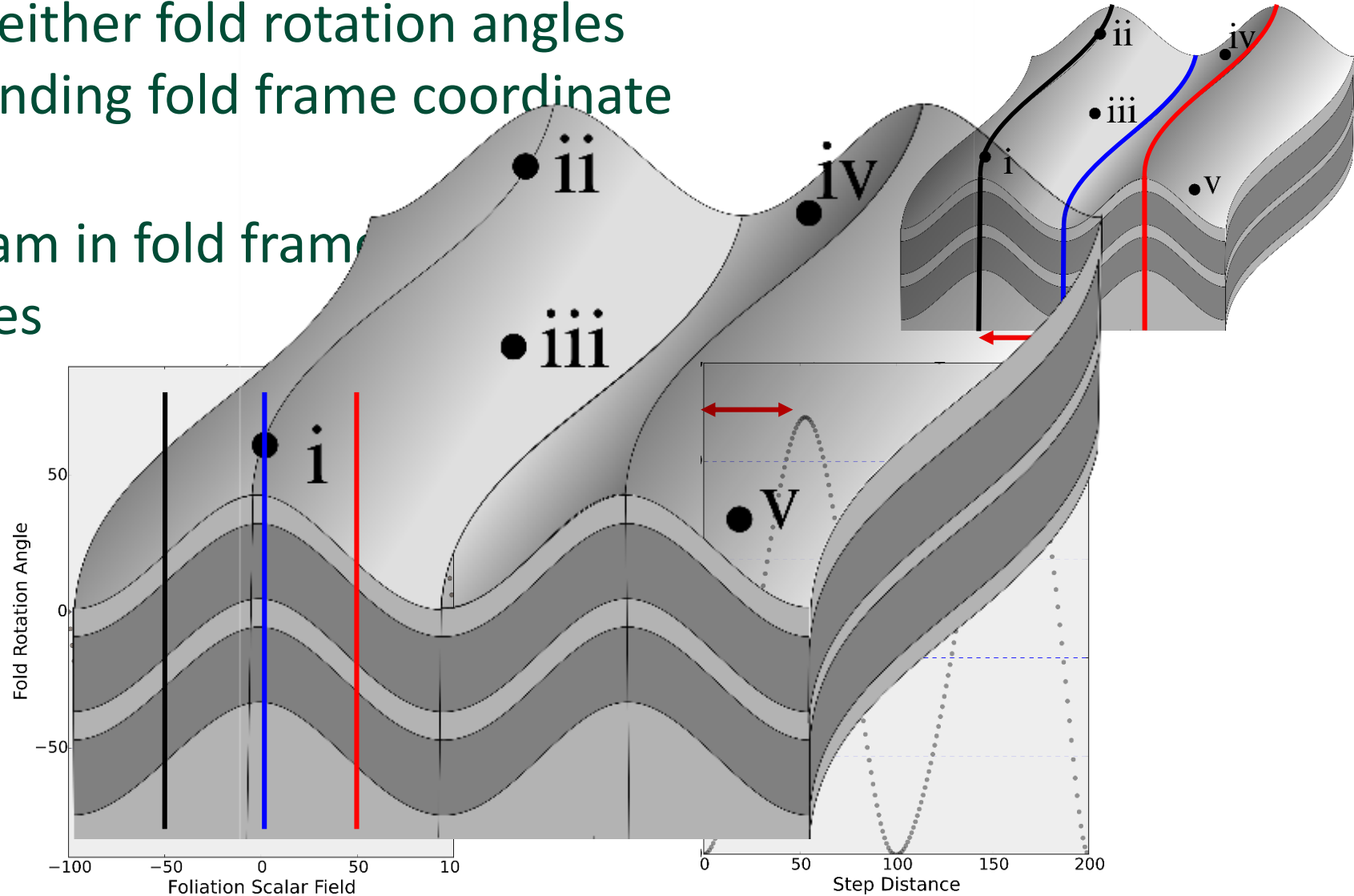
Classical Modelling



Orientation difference (degree)



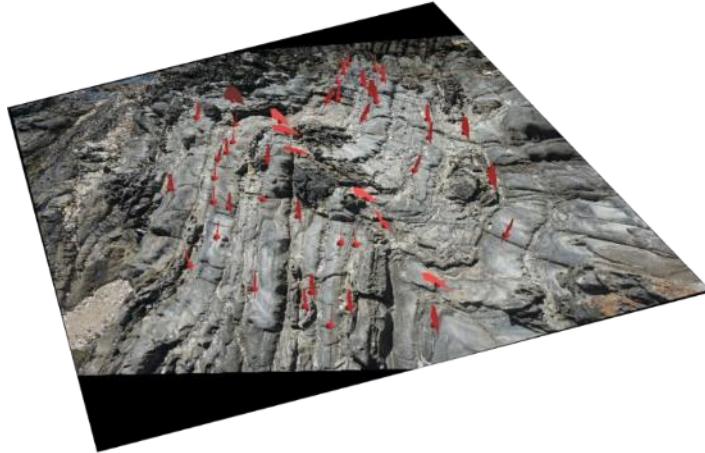
- S-Plot
  - Cross plot of either fold rotation angles and corresponding fold frame coordinate
- S-Variogram
  - Semi-variogram in fold frame rotation angles



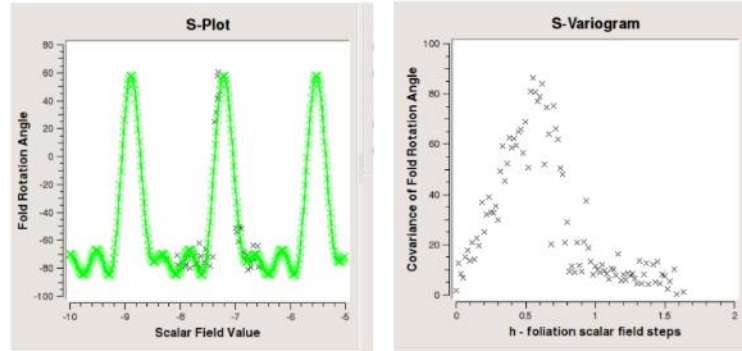
Accepted paper to J.  
Structural Geology:  
Structural Data  
Constraints for Implicit  
Modeling of Folds (Grose  
et al.)



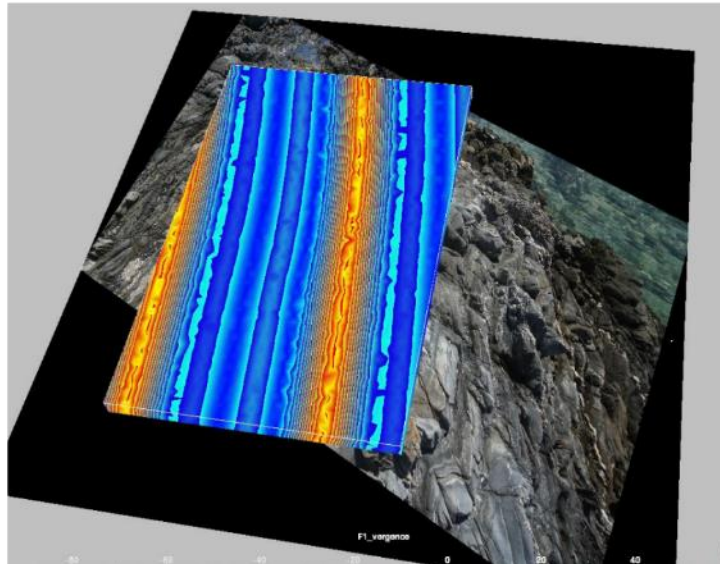
**A) Outcrop image with field observations**



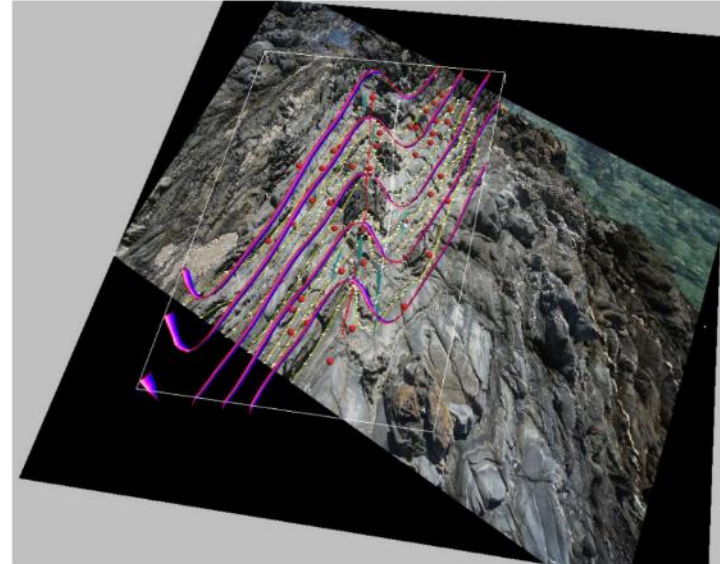
**B) Foliation plots: Left S-Plot of S1 and S0 with interpolate profile (green). Right S-variogram S1 and S0.**



**C) Fold limb rotation angle scalar field interpolated from B**



**D) Final geometrical model showing form surfaces for bedding**



(Grose et al., Laurent et al.)

